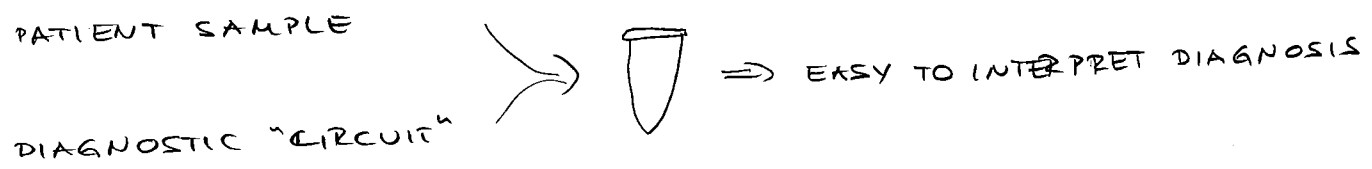


MOTIVATION

- TB DRUG RESISTANCE (DETECT DNA, USE PCR, ON PAPER, SNPs, ...)
- CANCER CLASSIFICATION BASED ON MIRNA (ssRNA, qPCR, COMPUTATIONAL, ...)
- FLU VIRUS IN CELLS (A. PAJ) (ssRNA, MICROSCOPY, ...)

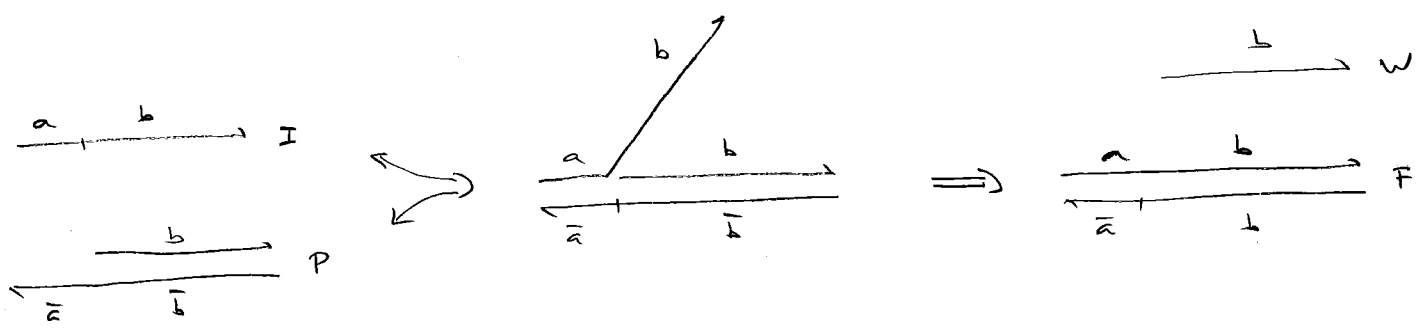
COMMON TO ALL : MULTIPLE INPUTS, HIGH SPECIFICITY REQUIRED, COMPLEX EXPERIMENTAL + ANALYSIS WORKFLOW.

BETTER ALTERNATIVE? MOLECULAR DIAGNOSTICS



APPROACH : DNA STRAND DISPLACEMENT

- ssDNA
- SD ANIMATION
- MODEL FOR SD : 2-STEP VS. 1-STEP (PRE-EQUILIBRIUM ANALYSIS)



$$\frac{d[F]}{dt} = +k_2 [C]$$

$$\frac{d[C]}{dt} = k_+ [I][P] - (k_- + k_2) [C] \stackrel{!}{=} 0$$

$$[C] = \frac{k_+}{k_- + k_2} [I][G]$$

$$\frac{d[P]}{dt} = \frac{k_2 k_+}{k_- + k_2} [I][G] = k [I][G] \quad (\sim \text{BIMOLECULAR})$$

STRONG TOEHOLD : $k_2 > k_-$

$$k = \frac{k_2 k_+}{k_- + k_2} \sim k_+ \Rightarrow \text{FIT DATA TO FIND } k_+!$$

(DIFFERENT FOR DIFFERENT TOEHOLDS!)

WEAK TOEHOLD : $k_2 < k_-$

$$k \approx \frac{k_2 k_+}{k_-} = k_2 \cdot C \cdot e^{-|\Delta G|/RT}$$

$$\left[\text{CHEMICAL EQ.} \quad K_{eq} = \frac{k_+}{k_-} = \frac{[I][G]}{[C]} = e^{-\Delta G/RT} \right]$$

ΔG IS THE FREE ENERGY OF TOEHOLD BINDING, CAN BE CALCULATED FROM FIRST PRINCIPLES.
TREAT k_2 AS A FITTING PARAMETER.

\Rightarrow IN CLASS WORKING SESSION: ① CALCULATE ΔG FOR DIFFERENT TOEHOLD LENGTH

	<table border="0"> <tr><td>n = 1</td><td>-1.52</td></tr> <tr><td>2</td><td>-3.36</td></tr> <tr><td>3</td><td>-4.79</td></tr> <tr><td>4</td><td>-6.74</td></tr> <tr><td>5</td><td>-8.1</td></tr> <tr><td>6</td><td></td></tr> </table>	n = 1	-1.52	2	-3.36	3	-4.79	4	-6.74	5	-8.1	6	
n = 1	-1.52												
2	-3.36												
3	-4.79												
4	-6.74												
5	-8.1												
6													

b : 5' CCTC CATT CAAT ACCCTACG

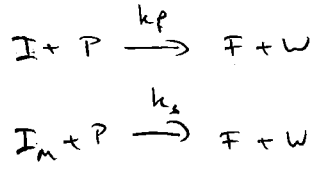
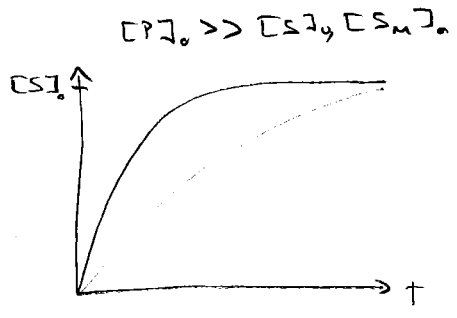
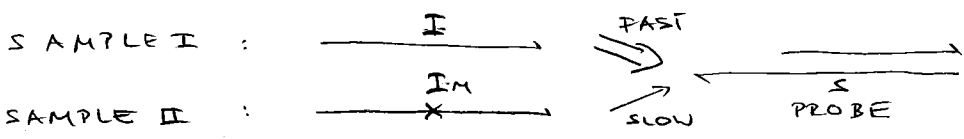
a : 5' CCACAT

② PLOT $\log_{10} k$ VS. ΔG , COMPARE TO DATA

③ CONSIDER MUTATIONS $\begin{matrix} \Delta G \\ \uparrow \uparrow \\ \text{CCACAT} \end{matrix}$

SNV DISCRIMINATION

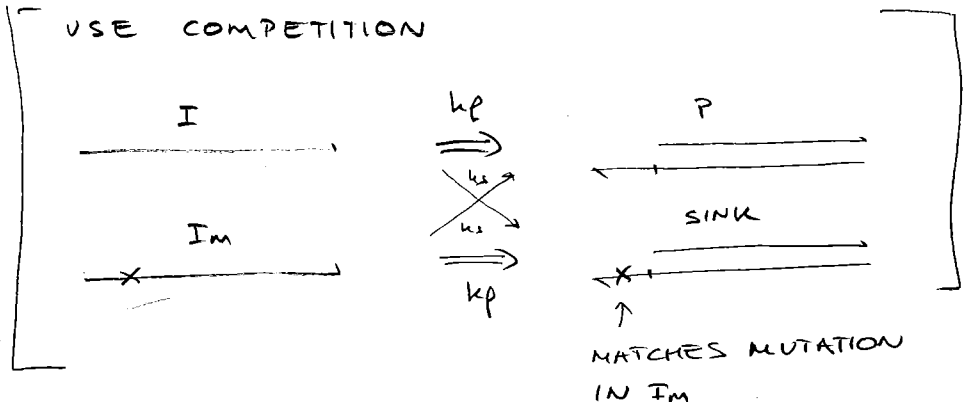
WE ALREADY KNOW THAT MUTATIONS AFFECT KINETICS.
 COULD THIS BE USED TO DETECT SNPs?



BUT

- NO CONTROL OVER CONCENTRATION
- NO DISCRIMINATION AT END POINT

USE COMPETITION



IDEAL PROBES ARE SPECIFIC + SENSITIVE

DISCRIMINATION FACTOR $DF = \frac{F}{F_M} = \frac{\text{SIGNAL WITH INPUT I}}{\text{SIGNAL WITH INPUT } I_M}$

[SAME CONC., ONLY ONE IS PRESENT]

DF IS A MEASURE OF PROBE SPECIFICITY.

YIELD $X = \frac{[F]}{[I]_0} = \frac{\text{SIGNAL}}{\text{INPUT CONCENTRATION}}$

SINGLE SD PROPE

DF = 1, X = 1 : NO SPE

$$\dot{[F]} = k_f [I][P] \approx k_f [P]_0 [I] = -k_f \frac{d[I]}{dt}$$

$$[I](t) = [I]_0 e^{-k_f [P]_0 t} \Rightarrow [F](t) = [I]_0 (1 - e^{-k_f [P]_0 t})$$

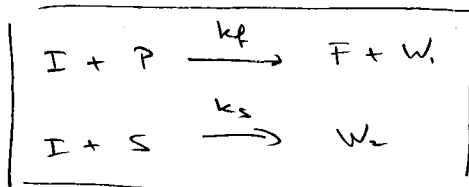
$$t \rightarrow \infty : [F]_{\infty} = [I]_0$$

SAME FOR $[I]_n$, JUST SLOWER.

$$DF_{\infty} = \frac{[F]_{\infty}}{[I]_n} = 1 \quad ; \quad \text{NOT SPECIFIC AT END POINT}$$

$$X = \frac{[F]}{[I]_n} = \frac{[I]_0}{[I]_0} = 1 \quad ; \quad \text{NOT (VERY) SENSITIVE}$$

COMPETITION :



$$\frac{d[F]}{dt} = k_f [I][P]_0$$

$$\frac{d[I]}{dt} \approx -k_f [I][P]_0 - k_s [I][S]_0 = -[I] \underbrace{(k_f [P]_0 + k_s [S]_0)}_{\Gamma}$$

$$[I](t) = [I]_0 e^{-\Gamma t}$$

$$\frac{d[F]}{dt} = k_f [I]_0 [P]_0 e^{-\Gamma t}$$

$$F(t) = C_0 - \frac{k_f [P]_0}{k_f [P]_0 + k_s [S]_0} [I]_0 e^{-\Gamma t}$$

$$[F](0) \stackrel{=0}{=} [I]_0 \frac{k_f [P]_0}{k_f [P]_0 + k_s [S]_0} (1 - e^{-\Gamma t})$$

$$[F]_{\infty} = [I]_0 \frac{k_f [P]_0}{k_f [P]_0 + k_s [S]_0} \quad [P]_0 = [S]_0$$

$$\downarrow$$

$$= [I]_0 \frac{k_f}{k_f + k_s}$$

RXN w/ I_M :

$$[F_M]_{\infty} = [I_M]_0 \frac{k_s [P]_0}{k_s [P]_0 + k_f [S]_0} \quad [P]_0 = [S]_0$$

$$\downarrow$$

$$= [I_M]_0 \frac{k_s}{k_f + k_s}$$

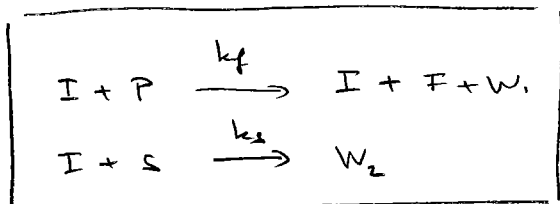
$$DF_{\infty} = \frac{[F]_{\infty}}{[F_M]_{\infty}} = \frac{k_f}{k_s}$$

Q1: HOW BIG IS THAT NBR?

Q2: WHAT IS MUTATION IS NOT IN THE TOLERANCE?

$$X_{\infty} = \frac{[F]_{\infty}}{[I]_0} = \frac{k_f}{k_f + k_s} < 1$$

CAN WE INCREASE THE YIELD BY MAKING THE INTENDED REACTION CATALYTIC? LET'S TRY:



STILL ASSUME $[P]_0 = [S]_0 \gg [I]$

RXNS CAN BE SOLVED ANALYTICALLY BUT HERE WE USE INTUITIVE ARGUMENT INSTEAD

$X = \frac{k_f}{k_f + k_s}$: PROB. OF SUCCESSFUL RXN IN ONE ROUND

$$[F]_{\infty} = [I]_0 (X + X^2 + X^3 + \dots) = \frac{X}{1-X} [I]_0$$

$$X_{\infty} = \frac{[F]_{\infty}}{[I]_0} = \frac{X}{1-X} = \frac{k_f}{k_f + k_s} \cdot \frac{k_f + k_s}{k_s} = \frac{k_f}{k_s} > 1$$

DISCRIMINATION FACTOR

HOW ABOUT I_M :

$$\text{PROB OF 1ST ROUND SUCCESS: } y = \frac{k_s}{k_f + k_s} = 1 - x$$

$$[F_M]_\infty = [I] \cdot (y + y^2 + y^3 + \dots) = \frac{y}{1-y} = \frac{1-x}{x}$$

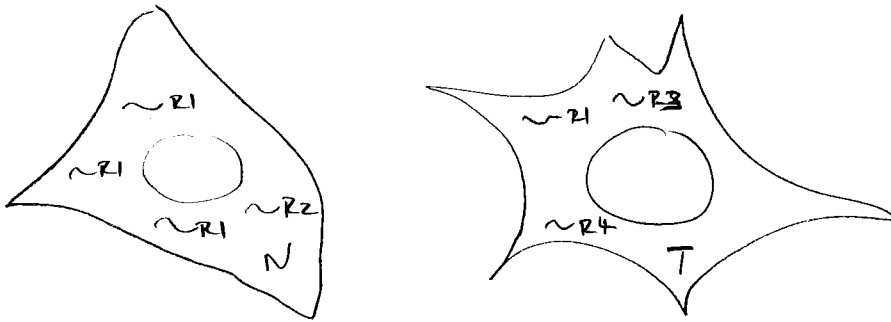
$$\underline{DF} = \frac{[F]_\infty}{[F_M]_\infty} = \left(\frac{x}{1-x} \right)^2 = \underline{(k_f/k_s)^2}$$

\Rightarrow QUADRATICALLY BETTER THAN FOR COMPETITION ALONE!

HOW CAN WE MAKE A CATALYST? \Rightarrow DNA STRAND DISPLACEMENT
CASCADES AND SEESAW
AMPLIFIERS

MULTI-ANALYTE DETECTION

GOAL: BUILD MOLECULAR CLASSIFIER

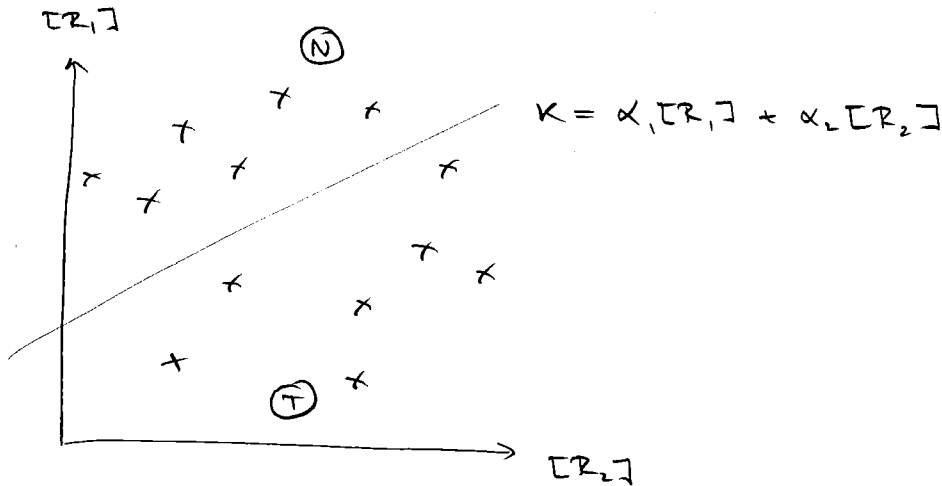


BOOLEAN CLASSIFIER:

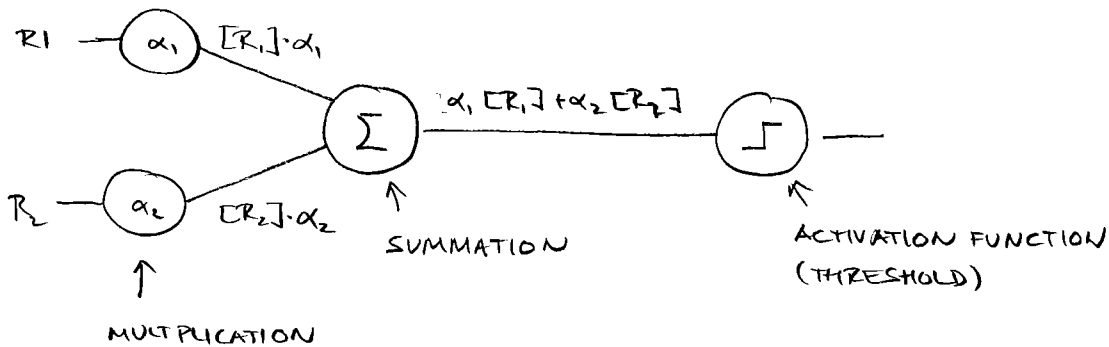
N: R₁ AND R₂

T: R₃ OR R₄

MORE COMMON: LOW/HIGH RATHER THAN ABSENCE/PRESENCE



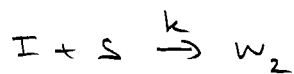
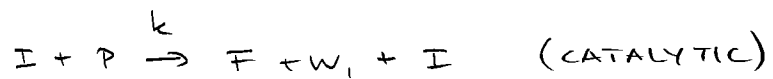
ANOTHER WAY TO REPRESENT THIS



CONSIDER MULTIPLICATION FIRST.

LET'S REVISIT COMPETITIVE INHIBITION!

BUT THIS TIME ASSUME $k_p = k_s = k$, $[P]_0 \neq [S]_0$, $[P]_0, [S]_0 \gg [I]_0$.



PROB. OF SUCCESS FOR ONE ROUND:

$$x = \frac{k[P]_0}{k[P]_0 + k[S]_0} = \frac{[P]_0}{[P]_0 + [S]_0}$$

TOTAL FLUORESCENCE AFTER MANY ROUNDS:

$$\underline{[F]} = [I]_0 \left(x + x^2 + \dots \right) = [I]_0 \frac{x}{1-x} = [I]_0 \underbrace{\frac{[P]_0}{[S]_0}}_{\alpha} = \underline{\alpha [I]_0}$$

MULTIPLICATION W/ ARBITRARY α CAN BE REALIZED BY SETTING THE INITIAL CONCENTRATIONS OF $[P]_0, [S]_0$ ACCORDINGLY!